

## Disclaimer 1 about D-Feedback: Lack of Causality

Consider some state-space models:

$$\dot{x} = Ax + Bu$$

$$sX = AX + BU$$

$$(s - A)X = BU$$

$$y = Cx$$

$$Y = CX$$

$$\frac{Y}{U} = \frac{CB}{s - A} \equiv \frac{q(s)}{p(s)}$$

$\deg(q) < \deg(p)$  — strictly proper transfer function

$$(s - A)X = BU$$

$$\dot{x} = Ax + Bu$$

$$sX = AX + BU$$

$$Y = \frac{CB}{s - A}U + DU$$

$$y = Cx + Du$$

$$Y = CX + DU$$

$$= \frac{CB + D(s - A)}{s - A}U \equiv \frac{q(s)}{p(s)}$$

$\deg(q) = \deg(p)$  — proper transfer function

Causal systems have proper transfer functions.