

Low-Order Cases ($n = 2, 3$)

$$n = 2 \quad p(s) = s^2 + a_1s + a_2$$

$$s^2 \quad : 1 \quad a_2$$

$$s^1 \quad : a_1 \quad 0$$

$$s^0 : \quad b_1$$

$$b_1 = -\frac{1}{a_1} \det \begin{pmatrix} 1 & a_2 \\ a_1 & 0 \end{pmatrix} = a_2$$

— p is stable iff $a_1, a_2 > 0$ (necessary *and* sufficient).

$$n = 3 \quad p(s) = s^3 + a_1s^2 + a_2s + a_3$$

$$s^3 \quad : 1 \quad a_2$$

$$s^2 \quad : a_1 \quad a_3$$

$$s^1 : \quad b_1 \quad 0$$

$$s^0 : \quad c_1$$

$$b_1 = -\frac{1}{a_1} \det \begin{pmatrix} 1 & a_2 \\ a_1 & a_3 \end{pmatrix} = \frac{a_1a_2 - a_3}{a_1}$$

$$c_1 = -\frac{1}{b_2} \det \begin{pmatrix} a_1 & a_3 \\ b_1 & 0 \end{pmatrix} = a_3$$

— p is stable iff $a_1, a_2, a_3 > 0$ (necc. cond.) and $a_1a_2 > a_3$