

Routh's Test

Problem: check whether the polynomial

$$p(s) = s^n + a_1 s^{n-1} + a_2 s^{n-2} + \dots + a_{n-1} s + a_n$$

is strictly stable.

We begin by forming the **Routh array** using the coefficients of p :

$$\begin{array}{l} s^n : \quad 1 \quad a_2 \quad a_4 \quad a_6 \quad \dots \\ s^{n-1} : \quad a_1 \quad a_3 \quad a_5 \quad a_7 \quad \dots \end{array} \quad \begin{array}{l} \text{(if necessary, add zeros in the} \\ \text{second row to match lengths)} \end{array}$$

Note that the very first entry is always 1, and also note the order in which the coefficients are filled in.