

2nd-Order Step Response

$$H(s) = \frac{\omega_n^2}{s^2 + 2\zeta\omega_n s + \omega_n^2} = \frac{\omega_n^2}{(s + \sigma)^2 + \omega_d^2}$$

$$u(t) = 1(t) \quad \longrightarrow \quad y(t) = 1 - e^{-\sigma t} \left(\cos(\omega_d t) + \frac{\sigma}{\omega_d} \sin(\omega_d t) \right)$$

where $\sigma = \zeta\omega_n$ and $\omega_d = \omega_n\sqrt{1 - \zeta^2}$ (damped frequency)

We will see that the parameters ζ and ω_n determine certain important features of the transient part of the above step response.

We will also learn how to pick ζ and ω_n in order to *shape* these features according to given *specifications*.