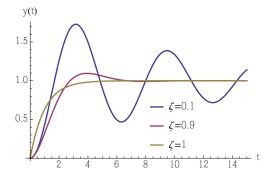
## 2nd-Order Step Response

$$H(s) = \frac{\omega_n^2}{s^2 + 2\zeta\omega_n s + \omega_n^2} = \frac{\omega_n^2}{(s+\sigma)^2 + \omega_d^2}$$
$$u(t) = 1(t) \qquad \longrightarrow \qquad y(t) = 1 - e^{-\sigma t} \left(\cos(\omega_d t) + \frac{\sigma}{\omega_d}\sin(\omega_d t)\right)$$

where 
$$\sigma = \zeta \omega_n$$
 and  $\omega_d = \omega_n \sqrt{1 - \zeta^2}$  (damped frequency)



The parameter  $\zeta$  is called the *damping ratio* 

- $\zeta > 1$ : system is overdamped
- $\zeta < 1$ : system is underdamped
- $\zeta = 0$ : no damping  $(\omega_d = \omega_n)$