State-Space Models

$$\dot{x} = Ax + Bu$$
$$y = Cx$$

where:

- $x(t) \in \mathbb{R}^n$ is the state at time t
- $u(t) \in \mathbb{R}^m$ is the input at time t
- $y(t) \in \mathbb{R}^p$ is the output at time t

and

- $A \in \mathbb{R}^{n \times n}$ is the dynamics matrix
- $B \in \mathbb{R}^{n \times m}$ is the control matrix
- $C \in \mathbb{R}^{p \times n}$ is the sensor matrix

How do we determine the output y for a given input u?

Reminder: we will only consider single-input, single-output (SISO) systems, i.e., $u(t), y(t) \in \mathbb{R}$ for all times t of interest. (m = p = 1)