

## Review: Controllability

Consider a single-input system ( $u \in \mathbb{R}$ ):

$$\dot{x} = Ax + Bu, \quad y = Cx \quad x \in \mathbb{R}^n$$

The **Controllability Matrix** is defined as

$$\mathcal{C}(A, B) = [B \mid AB \mid A^2B \mid \dots \mid A^{n-1}B]$$

We say that the above system is **controllable** if its controllability matrix  $\mathcal{C}(A, B)$  is *invertible*.

- ▶ As we will see today, if the system is controllable, then we may assign arbitrary closed-loop poles by *state feedback* of the form  $u = -Kx$ .
- ▶ Whether or not the system is controllable depends on its state-space realization.