

Controller Canonical Form

A single-input state-space model

$$\dot{x} = Ax + Bu, \quad y = Cx$$

is said to be in **Controller Canonical Form** (CCF) if the matrices A, B are of the form

$$A = \begin{pmatrix} 0 & 1 & 0 & \dots & 0 & 0 \\ 0 & 0 & 1 & \dots & 0 & 0 \\ \vdots & \vdots & \vdots & \ddots & \vdots & \vdots \\ 0 & 0 & 0 & \dots & 0 & 1 \\ * & * & * & \dots & * & * \end{pmatrix}, \quad B = \begin{pmatrix} 0 \\ 0 \\ \vdots \\ 0 \\ 1 \end{pmatrix}$$

A system in CCF is *always controllable!!*

(The proof of this for $n > 2$ uses the Jordan canonical form, we will not worry about this.)