

## CCF with Arbitrary Zeros

In our example, we had  $G(s) = \frac{s+1}{s^2+5s+6}$ , with a minimum-phase zero at  $z = -1$ .

Let's consider a general zero location  $s = z$ :

$$G(s) = \frac{s-z}{s^2+5s+6}$$

This gives us a CCF realization

$$\begin{pmatrix} \dot{x}_1 \\ \dot{x}_2 \end{pmatrix} = \underbrace{\begin{pmatrix} 0 & 1 \\ -6 & -5 \end{pmatrix}}_A \begin{pmatrix} x_1 \\ x_2 \end{pmatrix} + \underbrace{\begin{pmatrix} 0 \\ 1 \end{pmatrix}}_B u, \quad y = \underbrace{\begin{pmatrix} -z & 1 \end{pmatrix}}_C \begin{pmatrix} x_1 \\ x_2 \end{pmatrix}$$

Since  $A, B$  are the same,  $C(A, B)$  is the same  $\implies$  the system is still controllable.

A system in CCF is controllable for any locations of the zeros.