Stability from Frequency Response

$$R \xrightarrow{+} K \xrightarrow{} G(s) \xrightarrow{} Y$$

Stability from frequency response. If $s = j\omega$ is on the root locus (for some value of K), then

$$|KG(j\omega)| = 1$$
 and $\angle KG(j\omega) = 180^{\circ} \mod 360^{\circ}$

Therefore, the transition from stability to instability can be detected in two different ways:

- from root locus as $j\omega$ -crossings
- From Bode plots as M = 1 and φ = 180° at some frequency ω (for a given value of K)