Stability from Frequency Response

$$R \xrightarrow{+} K \xrightarrow{} G(s) \xrightarrow{} Y$$

Question: How can we decide whether the *closed-loop* system is stable for a given value of K > 0 based on our knowledge of the *open-loop* transfer function KG(s)?

Another answer: let's look at the Bode plots:

$$\omega \longmapsto |KG(j\omega)|$$
 on log-log scale
 $\omega \longmapsto \angle KG(j\omega)$ on log-linear scale

— Bode plots show us magnitude and phase, but only for $s=j\omega,\, 0<\omega<\infty$

How does this relate to the root locus? $j\omega$ -crossings!!