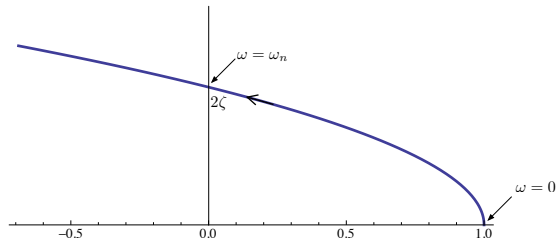


Type 3: $\left(\frac{j\omega}{\omega_n}\right)^2 + 2\zeta\frac{j\omega}{\omega_n} + 1$, Phase



Nyquist plot
($0 < \omega < \infty$)

$(R(\omega), I(\omega))$

$$= \left(1 - \left(\frac{\omega}{\omega_n}\right)^2, 2\zeta\frac{\omega}{\omega_n} \right)$$

Phase:

- ▶ for $\omega \ll \omega_n$, $\phi \approx 0^\circ$ (real and positive)
- ▶ for $\omega = \omega_n$, $\phi = 90^\circ$ (Re = 0, Im > 0)
- ▶ for $\omega \gg \omega_n$, $\phi \approx 180^\circ$ (Re $\sim -\omega^2$, Im $\sim \omega$)

For a stable complex zero, the phase steps up by 180° as we go through the breakpoint; as $\zeta \rightarrow 0$, the transition through the break-point gets sharper, almost step-like.

For a pole, the phase is multiplied by -1 .