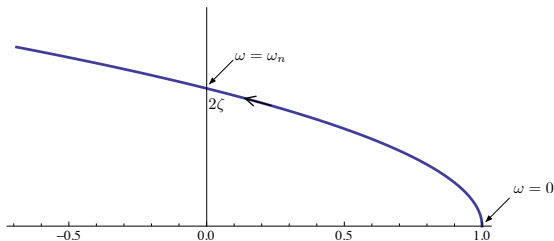


Type 3: $\left(\frac{j\omega}{\omega_n}\right)^2 + 2\zeta\frac{j\omega}{\omega_n} + 1$, Magnitude



Nyquist plot
($0 < \omega < \infty$)

$$(R(\omega), I(\omega)) \\ = \left(1 - \left(\frac{\omega}{\omega_n}\right)^2, 2\zeta\frac{\omega}{\omega_n} \right)$$

Magnitude:

- ▶ for $\omega \ll \omega_n$, $M \approx 1$ (horizontal line)
- ▶ for $\omega \gg \omega_n$, $M \approx \left(\frac{\omega}{\omega_n}\right)^2 \Rightarrow \log M \approx 2 \log \omega - 2 \log \omega_n$
The asymptote is a line of slope 2 passing through the point ($\omega = \omega_n, M = 1$)

For a stable complex zero, the magnitude slope steps up by 2 as we go through the breakpoint.