Example

PD control of an unstable 2nd-order plant

$$R \xrightarrow{+} G_c \xrightarrow{K_P + K_D s} \xrightarrow{1} G_p Y$$

$$\frac{Y}{R} = \frac{G_cG_p}{1+G_cG_p} \qquad \text{poles: } 1+G_c(s)G_p(s)=0$$

$$1+(K_{\text{P}}+K_{\text{D}}s)\left(\frac{1}{s^2-1}\right)=0$$

We will examine the impact of varying $K = K_D$, assuming the ratio K_P/K_D fixed.