

EM Algorithm for PLSA: E-Step

Hidden Variable (=topic indicator): $z_{d,w} \in \{B, 1, 2, \dots, k\}$

Probability that **w** in doc **d** is generated from **topic** θ_j

$$p(z_{d,w} = j) = \frac{\pi_{d,j}^{(n)} p^{(n)}(w | \theta_j)}{\sum_{j'=1}^k \pi_{d,j'}^{(n)} p^{(n)}(w | \theta_{j'})}$$

Use of Bayes Rule

$$p(z_{d,w} = B) = \frac{\lambda_B p(w | \theta_B)}{\lambda_B p(w | \theta_B) + (1 - \lambda_B) \sum_{j=1}^k \pi_{d,j}^{(n)} p^{(n)}(w | \theta_j)}$$

↑
Probability that **w** in doc **d** is generated from **background** θ_B