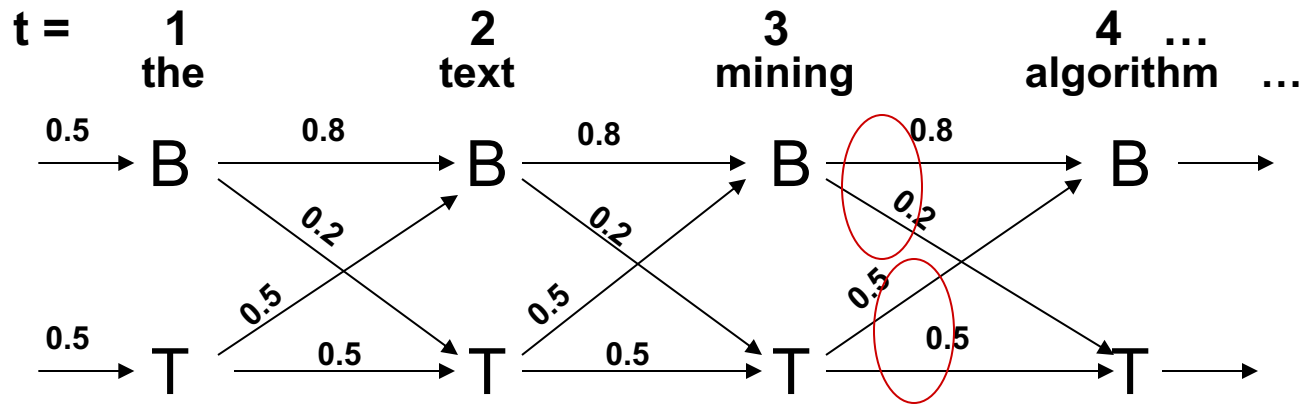


Backward Algorithm: Example

$$p(o_1 \dots o_T | \lambda) = \sum_{i=1}^N \pi_i b_i(o_1) \beta_1(i) = \sum_{i=1}^N \alpha_1(i) \beta_1(i) = \sum_{i=1}^N \alpha_t(i) \beta_t(i) \text{ for any } t$$



$$\dots \quad \beta_3(\mathbf{B}): 0.8 \cdot p(\text{"alg"}|\mathbf{B}) \beta_4(\mathbf{B}) + 0.2 \cdot p(\text{"alg"}|\mathbf{T}) \beta_4(\mathbf{T}) \quad \beta_4(\mathbf{B}): 1$$

$$\dots \quad \beta_3(\mathbf{T}): 0.5 \cdot p(\text{"alg"}|\mathbf{B}) \beta_4(\mathbf{B}) + 0.5 \cdot p(\text{"alg"}|\mathbf{T}) \beta_4(\mathbf{T}) \quad \beta_4(\mathbf{T}): 1$$

$$\begin{aligned} P(\text{"the text mining algorithm"}) &= \alpha_1(\mathbf{B}) \beta_1(\mathbf{B}) + \alpha_1(\mathbf{T}) \beta_1(\mathbf{T}) \\ &= \alpha_2(\mathbf{B}) \beta_2(\mathbf{B}) + \alpha_2(\mathbf{T}) \beta_2(\mathbf{T}) \end{aligned}$$