...we choose to use the sum $\mathbf{W} + \tilde{\mathbf{W}}$ *as our word vectors.*

word2vec *also* learns $\tilde{\mathbf{W}}$! Why not do the same for both?