

Likelihood Functions for PLSA vs. LDA

PLSA

$$p_d(w | \{\theta_j\}, \{\pi_{d,j}\}) = \sum_{j=1}^k \pi_{d,j} p(w | \theta_j)$$

**Core assumption
in all topic models**

$$\log p(d | \{\theta_j\}, \{\pi_{d,j}\}) = \sum_{w \in V} c(w, d) \log \left[\sum_{j=1}^k \pi_{d,j} p(w | \theta_j) \right]$$

$$\log p(C | \{\theta_j\}, \{\pi_{d,j}\}) = \sum_{d \in C} \log p(d | \{\theta_j\}, \{\pi_{d,j}\})$$

LDA

$$p_d(w | \{\theta_j\}, \{\pi_{d,j}\}) = \sum_{j=1}^k \pi_{d,j} p(w | \theta_j)$$

PLSA component

$$\log p(d | \bar{\alpha}, \{\theta_j\}) = \int \left[\sum_{w \in V} c(w, d) \log \left[\sum_{j=1}^k \pi_{d,j} p(w | \theta_j) \right] \right] p(\bar{\pi}_d | \bar{\alpha}) d\bar{\pi}_d$$

$$\log p(C | \bar{\alpha}, \bar{\beta}) = \int \sum_{d \in C} \log p(d | \bar{\alpha}, \{\theta_j\}) \prod_{j=1}^k p(\theta_j | \bar{\beta}) d\theta_1 \dots d\theta_k$$

Added by LDA