

# Linear SVM with Soft Margin

**Classifier:**  $f(\mathbf{x}) = \mathbf{w}^T \mathbf{x} + b > 0$ ?

**Parameters:**  $\mathbf{w}$ ,  $b$

**Training Data:**  $T = \{(\mathbf{x}_i, y_i)\}, i=1, \dots, |T|$ .

**Find  $\mathbf{w}$ ,  $b$ , and  $\xi_i$  to minimize**  $\Phi(\mathbf{w}) = \mathbf{w}^T \mathbf{w} + C \sum_{i \in [1, |T|]} \xi_i$

Added to allow training errors



**Subject to**  $\forall i \in [1, |T|], y_i(\mathbf{w}^T \mathbf{x}_i + b) \geq 1 - \xi_i, \quad \xi_i \geq 0$

$C > 0$  is a parameter to control the trade-off between minimizing the errors and maximizing the margin

**The optimization problem is still quadratic programming with linear constraints**