

Negation, again

Negate: $(x \rightarrow y) \wedge \neg x$

Second Solution: We begin by simplifying the expression above before negating it. Note that

$$x \rightarrow y \equiv \neg x \vee y$$

Hence

$$\begin{aligned}(x \rightarrow y) \wedge \neg x & \\ \equiv (\neg x \vee y) \wedge \neg x & \\ \equiv (\neg x \wedge \neg x) \vee (y \wedge \neg x) & \\ \equiv \neg x \vee (y \wedge \neg x) & \\ \equiv \neg x & \end{aligned}$$

Therefore,

$$\neg[(x \rightarrow y) \wedge \neg x] \equiv \neg\neg x \equiv x$$