

## Simplifications (warm-up)

When  $A$  and  $B$  are logical expressions, and you say  $A \equiv B$ , you mean that they have the same truth values. (You can also write this as  $A \leftrightarrow B$ .)

For example:

▶  $\neg\neg x \equiv x$  (obvious)

▶  $x \vee (x \wedge y) \equiv x$

Similarly, you can write  $x \vee (x \wedge y) \leftrightarrow x$ . In other words,  $x \vee (x \wedge y)$  is true if and only if  $x$  is true.

▶  $x \vee \neg x \equiv T$

In other words,  $x \vee \neg x$  is always true, no matter what  $x$  is.

▶  $x \wedge \neg x \equiv F$

In other words,  $x \wedge \neg x$  is never true, no matter what  $x$  is.