

## Using strong induction

Let  $F : \mathbb{Z}^+ \rightarrow \mathbb{Z}$  be defined by

- ▶  $F(1) = 1$  and  $F(2) = 0$
- ▶  $F(n) = F(n - 2)$  if  $n > 2$

Then  $F(n) = n \bmod 2$  for all  $n \in \mathbb{Z}^+$ .

Let  $P(k)$  be the assertion:

- ▶  $F(k) = k \bmod 2$

and let us assume that  $P(1), P(2), \dots, P(n)$  are all true.

We need two base cases  $n = 1$  and  $n = 2$ .

Does this work? (YES)

Why do we need two base cases? (You'll see later)