Our induction proof has failed!

Our Inductive Hypothesis only told us about $F(n)$, not about $F(n-1)$.

Our induction proof failed because we don't know anything about $F(n-1)$.

We need to make a statement about *all* preceeding values, not just the immediate predecessor.