

Very easy induction proof

Our base case is $n = 0$, and asserts that $f(0) = 0$, which is true.