## Recursively defined set

• 
$$S_0 = \emptyset$$

• 
$$S_n = S_{n-1} \cup \{n\}$$
 for  $n \ge 1$ .

Theorem:  $\forall n \in \mathbb{Z}^+$ ,  $S_n = \{x \in \mathbb{Z}^+ | x \le n\} = \{1, 2, \dots, n\}.$ 

We will prove this two ways:

- First proof is by contradiction.
- Second proof is by induction.