

# $\mathcal{NP}$ -hard

We use the fact that 3-colorability is  $\mathcal{NP}$ -hard to prove that 4-colorability is  $\mathcal{NP}$ -hard.