

# Karp Reductions

Suppose  $\pi' \in \mathcal{P}$ , and that  $\mathcal{A}$  is a polynomial time algorithm to solve  $\pi'$ .

Suppose  $\pi \propto \pi'$ , and that  $F$  is the Karp Reduction.

Given instance  $I$  to  $\pi$ ,

- ▶ Compute  $F(I)$ , which is an instance of  $\pi'$ .
- ▶ Run algorithm  $\mathcal{A}$  on  $F(I)$
- ▶ If  $\mathcal{A}$  says YES, then return YES; otherwise return NO.

So: if you can find a Karp Reduction from  $\pi$  to  $\pi'$ , then if  $\pi'$  can be solved in polynomial time then so can  $\pi$ !