

# Karp Reductions

Suppose you have two decision problems,  $\pi$  and  $\pi'$ .

Suppose  $\pi' \in \mathcal{P}$ , and that  $\mathcal{A}$  is a polynomial time algorithm to solve  $\pi'$ .

Suppose we have a function  $F$  that maps inputs to  $\pi$  to inputs to  $\pi'$ , so that:

- ▶ YES-instances of  $\pi$  map to YES-instances of  $\pi'$
- ▶ NO-instances of  $\pi$  map to NO-instances of  $\pi'$
- ▶ The function  $F$  takes polynomial time to compute
- ▶ The size of  $F(I)$  is polynomial in the size of  $I$  for any input  $I$

Such a function  $F$  is called a *Karp* reduction, after Dick Karp (Berkeley) who came up with them.