Important points

Question: Suppose $\lim_{n \to \infty} \frac{f(n)}{g(n)} = \infty$. Does it follow that f is not $O(g)$?

Answer: YES! If the limit of the ratio is ∞, then it is not possible for f to be $O(g)$.