Finding a Longest Increasing Substring

Input: sequence (or array) $X = x_1x_2...x_n$ of integers Output: increasing substring of X that is as long as possible.

What is a substring?

▶ A substring is a string that begins at some x_i and ends at some x_j (with $j \ge i$) and includes all the intermediate elements.

For example, x_2, x_3, x_4 is a substring but x_2, x_4 is not.

Suppose X = 1, 3, 1, 8, 2, 4, 9, 2, 10, 3.

- What are some increasing substrings?
- ▶ What are some increasing subsequences?